

# Progressive Education Society's Modern College of Arts, Science & Commerce Ganeshkhind, Pune – 16

Even Semester Examination: April 2023-2024 Faculty: Science and Technology

Program: BSc Comp05 Semester: IV Set : B

Program (Specific):B.Sc. Computer Science
Class: S.Y.B.Sc(Comp. Sci.)

Course Type: Core
Max. Marks: 35

Name of the Course: Computational Geometry
Paper no.: I

Course Code: 23-MTC-241
Time: 2Hrs

#### Instructions to the candidate:

1) There are 3 sections in the question paper. Write each section on separate page.

2) All Sections are compulsory.

3) Figures to the right indicate full marks.

4) Draw a well labelled diagram wherever necessary.

#### **SECTION: A**

Q1. Attempt any five of the following:

(10 marks)

- a) Reflect the point [3 -2] through the line y=-x.
- b) What is the transformation matrix of rotation about origin through an angle 45° in clockwise direction?
- c) Write the transformation matrix for shearing in y- direction proportional to x and z co-ordinate by 1.5 and -2 units respectively, apply it on the point P[-2 5 7].
- d) Is the following matrix [T] a solid body transformation? Justify.

$$[T] = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ -1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix}$$

- e) Obtain the transformation matrix for a Cavalier projection for  $\alpha = 45^{\circ}$ .
- f) Define a foreshortening factor. Write the principal foreshortening factors for isometric projection.
- g) Determine the value of y on the unit circle if x=0.866.

### **SECTION: B**

Q2. Attempt any three of the following:

(15 marks)

- a) Find the combined transformation for following sequence of transformations:
  - i. Reflection in XY-plane
  - ii. Translate in x, y, z direction by 4,2,1 units respectively.
  - iii. Shearing in x co-ordinate by a factor -4 units proportional to z-co-ordinate.
- b) If If the line y=mx+h is transformed onto the line y\* =m\*x\* + h\* under the transformation matrix  $[T] = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$  then prove that  $m^* = (\frac{b+dm}{a+cm})$ .
- c) Find dimetric projection of the point P(2.5, 3.6, -5.1) with foreshortening factor  $f_z = \frac{2}{3}$ .
- d) Rotate the triangle ABC about its centroid through an angle  $45^{\circ}$ , where A[2 -4], B[3 0] and C[-2 1].
- e) Determine through what angles the plane X+Y+Z=0 be rotated about the X-axis and then about the Y-axis, so that it coincides with the Z=0 plane.

## **SECTION: C**

Q3. Attempt any one of the following:

(10 marks)

- a) Find the equi-spaced points on the circle  $x^2 + y^2 = 9$  (Take n=10).
- b)
- i) Find the parametric equation of Be'zier curve determined by control points  $B_o[2\ 1]$ ,  $B_1[4\ 3]$  and  $B_2[6\ 0.5]$  and hence find the position vector of the point corresponding to the parametric values t=0.43.
- ii) Write an algorithm for reflection through the line y=mx+c.